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## Modeling Flow Behavior of Sintered Al–4%B<sub>4</sub>C Composite During High–Temperature Upsetting

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### Abstract

The hot deformation behavior of sintered Al–4%B<sub>4</sub>C composites was studied in this work. The main aim of this work is to estimate the effect of initial relative density (IRD), deformation temperature and strain rate on the hot deformation behavior and development of constitutive equations for predicting the hot deformation behavior. For this purpose, upsetting was performed in a hydraulic press for obtaining true stress–true strain curve data of sintered Al–4%B<sub>4</sub>C composites. The tests were carried out at different IRDes of 80%, 85% and 90% for various temperatures of 573 K, 673 K and 773 K and strain rates of 0.1 s<sup>-1</sup>, 0.2 s<sup>-1</sup> and 0.3 s<sup>-1</sup>. The test reveals that the effect of IRD, deformation temperature and strain rate on flow stress curves is significant. The constitutive equations have been developed for predicting the flow stress behavior during the hot upsetting of sintered Al–4%B<sub>4</sub>C composite and it's validated with experiments. In addition, the required activation energies (Q) of sintered Al–4%B<sub>4</sub>C composites during the hot

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3 upsetting were calculated for various IRDes of 80%, 85%, and 90% was 161.06, 172.28 and 181.05  
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5 KJ/mol, respectively, which is higher than the value of pure aluminum (144.3 KJ/mol).  
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8 **Keywords:** Al-4%B<sub>4</sub>C composite, Flow stress, Constitutive modeling, Hot upsetting, Activation  
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10 energy.  
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## 14 **1. Introduction**

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17 The metal matrix composite (MMC) materials have been used in several engineering  
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19 applications successfully due to their attractive properties for the past four decades. MMCs  
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21 properties such as specific stiffness, strength, creep resistance and wear resistance can be enhanced  
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23 by adding selected reinforcement materials. In general, MMCs are fabricated by powder  
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25 metallurgy (P/M) technique, which is demonstrated to be effective in reducing the defects and  
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27 limitations of casting routes and also produce material with good quality properties. P/M technique  
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29 is more being used in several engineering applications at large scale because of its less material  
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31 utilization, less cost, less time, energy efficient operation and ease of automation. Cambronero et  
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33 al. [1] reported that the physical and mechanical properties of AA7075 aluminium alloy with  
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35 ceramic particle reinforcement were enhanced more, which are manufactured by the powder  
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37 metallurgy process, for automobile applications. Nair et al. [2] stated that Al and its alloys  
38  
39 reinforced with ceramic particles, which results in increased strength and reduced weight for the  
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41 structural applications. Abenojar et al. [3] described the suitability of boron for nuclear  
42  
43 applications due to its neutron absorption property. Boron carbide is one the hardest and lighter  
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45 (density = 2.51 g/cc) material than other commercial reinforcement. B<sub>4</sub>C is widely used as cermets  
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47 and armor materials due to good wear resistance properties. William and Harrigan [4] studied the  
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49 mechanical and thermal properties of aluminium matrix reinforced with B<sub>4</sub>C particles. It is  
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3 observed that the mechanical and thermal properties are enhanced by incorporating  $B_4C$  particles  
4 in aluminium matrix and the product cost is reduced when it is prepared by vacuum-hot pressing.  
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6 There is increasing interest in Al- $B_4C$  composites due to high hardness and strength to weight  
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8 ratio. An Al- $B_4C$  composite is used in defense, electronic and nuclear industries.  
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13 In the past few years, researchers are concentrating on the flow behavior of aluminium and  
14 its alloys for understanding the mechanical working processes. The knowledge about the hot  
15 deformation performance of the material is essential for optimizing the process parameters to get  
16 the desired products with excellent properties in the forming process. The flow stress of the  
17 material is influenced by deformation conditions such as temperature, strain, strain rate,  
18 microstructure of initial materials, and composition of the materials. Generally, the flow stress of  
19 the material can affect the required energy for forming and microstructure through the work  
20 hardening (WH), dynamic recovery (DRV) and dynamic recrystallization (DRX) in the hot  
21 deformation process. Several researches are conducted the experimental work on Al alloys and  
22 MMC to study the hot deformation behavior during a compression test. They have been studied  
23 the flow stress behavior and developed the constitutive models to predict the flow stress behavior  
24 for various deformation conditions [5-13]. Seetharam et al. [14-17] studied the workability,  
25 densification and hardness behavior of sintered Al- $B_4C$  composite and developed the  
26 mathematical models to predict the grain size of the composite.  
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46 The modeling of the constitutive equation of hot deformation is necessary for estimating  
47 the failure, understanding the phenomenon, the cost of design, and the lifetime of the product.  
48 Thus, many studies have been performed on wrought metals and its alloys as well as powder metals  
49 and reported the flow behavior while hot upsetting of the same. Hence, it is essential to investigate  
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3 the deformation process, flow stress behavior and development of a constitutive model with  
4 various process parameters for better performance of the metals.  
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8 Narayan and Rajeshkannan [18] performed cold upsetting tests on sintered iron–0.35%  
9 carbon to study densification behavior. They mentioned that the deformation behavior of the  
10 materials fabricated by powder metallurgy route is different from that of the cast/wrought materials  
11 (fully dense) because of the presence of more numbers of pores in the powder preforms, thereby  
12 limiting the deformation of the materials. Further, the volume of the pores is minimized during the  
13 deformation of sintered powder compacts this increasing density. Besides, Narayanasamy et al.  
14 [19] conducted cold upsetting tests on aluminium–3.5% alumina to study the effect of hardening  
15 on workability and densification. They discussed that the WH and flow stress of the materials is  
16 increased during the plastic deformation process, thus the sintered powder compacts undergo  
17 geometric hardening and densification hardening. Venugopal et al. [20] conducted ring–  
18 compression tests on sintered iron preforms for various relative densities. They found that the  
19 friction between works and tools is more in the powder preforms.  
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37 The limited work related to the hot upsetting behavior of sintered material by considering  
38 the IRD and deformation conditions is found. The information regarding the hot deformation  
39 performance of sintered Al–B<sub>4</sub>C composite is limited. Hence, the experimental works have been  
40 conducted on sintered Al–4%B<sub>4</sub>C composite to study the flow stress behavior for various IRDes  
41 and various deformation conditions during hot upsetting. The constitutive model was developed  
42 in terms of IRD of sintered Al–4%B<sub>4</sub>C composite to predict flow stress. The activation energy of  
43 sintered Al–4%B<sub>4</sub>C composite was calculated for different IRDes and compared with existing  
44 literature.  
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## 2. Materials and experimental procedures

The average particle size of aluminium powder is 45  $\mu\text{m}$  and purchased from SR Laboratories, Mumbai, India. Its purity is 99% and irregular in shape as shown in Figure. 1a. The ceramic reinforcement of boron carbide average size is 45  $\mu\text{m}$  and procured from supertek dies, Delhi, India. It is irregular morphology in nature as shown in Figure. 1b. Al powder and 4%B<sub>4</sub>C were carefully blended to get a homogenous mix in a pot mil about 60 min. The blended Al–4%B<sub>4</sub>C powder was compacted with a diameter and height of 15 mm. The various IRDes of preforms is obtained by applying different compaction load and to minimize the friction between punch and die Zinc stearate is used as a lubricant. Further, the green preforms were sintered in an electric muffle furnace for a period of 1 hr. at  $550 \pm 10$  °C followed by cooling at room temperature. The initial diameter and height of sintered preforms and density were measured by using Vernier calipers and Archimedes's principle, respectively. The hot upset test was conducted on the hydraulic press (capacity of 50 tons) between two flat dies at various temperatures of 573 K, 673 K and 773 K and strain rates of 0.1, 0.2 and 0.3 s<sup>-1</sup> and for IRDes of 80%, 85% and 90%. During the compression test, cylindrical compacts were heated for 30 min. (Soaking time) at test temperature to have a homogenous temperature. The progressive loads were applied to the cylindrical compacts until the appearance of first visible cracks on the circumference of the compacts. From the data–log unit of the hydraulic press the load-displacement data are recorded.

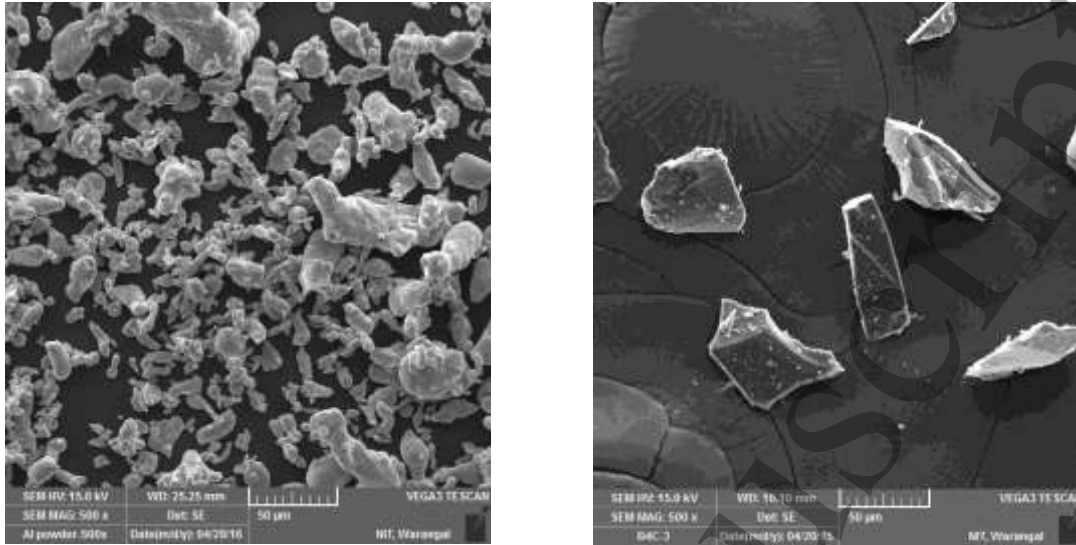


Figure. 1a SEM image of aluminium powder. Figure. 1b SEM image of boron carbide powder.

### 3. Results and discussion

#### 3.1. Hot deformation curves

The true stress ( $\sigma$ ) – true strain ( $\epsilon$ ) curves of sintered Al–4%B<sub>4</sub>C preforms with different IRDes for various temperatures and strain rate have been demonstrated in Figures. 2– 4. It is noted that the flow stress is varied for different temperatures, strain rates, and IRDes. Figure. 2a shows the relationship between  $\sigma$ – $\epsilon$  of sintered Al–4%B<sub>4</sub>C preforms with IRD of 80% and strain rate of 0.1 s<sup>-1</sup> for various temperatures such as 573 K, 673 K, and 773 K. It is noticed that the flow stress decreased with increasing temperature because of thermal softening and highest flow stress was found at low temperature. A similar kind of behavior is noticed for other preforms irrespective of strain rates and IRD of sintered Al–4%B<sub>4</sub>C preforms in Figures. 2–4. The flow stress difference is more between 673 K and 773 K for 80% IRD irrespective of the strain rate. During the upsetting process with lower IRD, the dislocation movement increases with increasing forming temperature and it is probably peak at 773 K. In Figure. 2, the graphs have been drawn between  $\sigma$ – $\epsilon$  with IRD of 80% for various temperatures and strain rates. It is noticed that the flow stress increased with

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3 increasing strain rate because the resistance offered by the material is increased in the preforms  
4 with increasing strain rate; hence to deform the material higher load is needed. A similar kind of  
5 behavior is noticed in the remaining IRD of 85% and 90% preforms as shown in Figures. 3 and 4  
6 respectively. Further, it is noticed that the flow stress is increased with an increasing the IRD of  
7 the composite irrespective of the temperatures and strain rates. The reason is that the strength of  
8 the composite is increased with an increasing IRD hence more deformation load is required to  
9 deform the material thus increase the flow stress [17].  
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20 At the initial stage, the  $\sigma$ - $\epsilon$  curves increase rapidly and then exhibit peak flow stress  
21 (PFS) at certain strain values after that it is constant until the end of the strain values due to work  
22 hardening and dynamic softening [21]. Sun et al. [11] revealed that in the early part of the  
23 deformation curves, dislocations multiplied considerably and the work hardening mechanism  
24 plays an important role which leads to a rapid increase in flow stress for smaller strain values. The  
25  $\sigma$ - $\epsilon$  curves are controlled by the work hardening before starting the DRX. After the PFS value, the  
26  $\sigma$ - $\epsilon$  curves become constant until higher strain values thus show the dynamic softening process.  
27 DRX phenomenon is followed by the DRV, which is described that the WH rate decreased with  
28 increasing strains values. According to Taleghani et al. [6], during hot upsetting the hardening and  
29 softening mechanism are happening in the powder preforms at a higher temperature. Irrespective  
30 of the IRD the dynamic softening has more at higher temperature and lower strain rate due to the  
31 mobility of grain boundaries increases and it accelerated the growth of DRX grains at the same  
32 condition [22]. Moreover, the effect of work hardening mechanism is partially or completely  
33 neutralized at higher strain values.  
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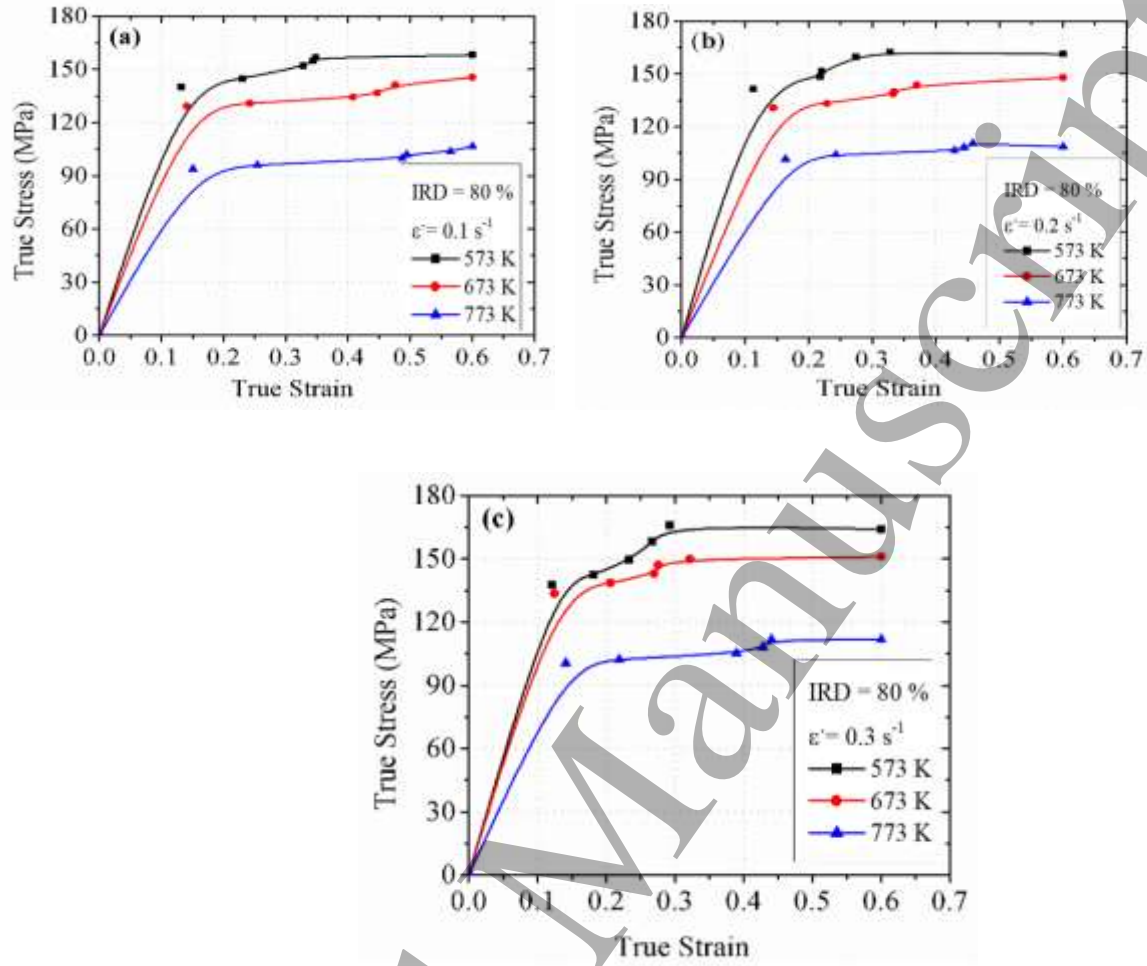


Figure. 2 True stress–true strain curves at various strain rate of Al-4%B<sub>4</sub>C composite with of 80%.

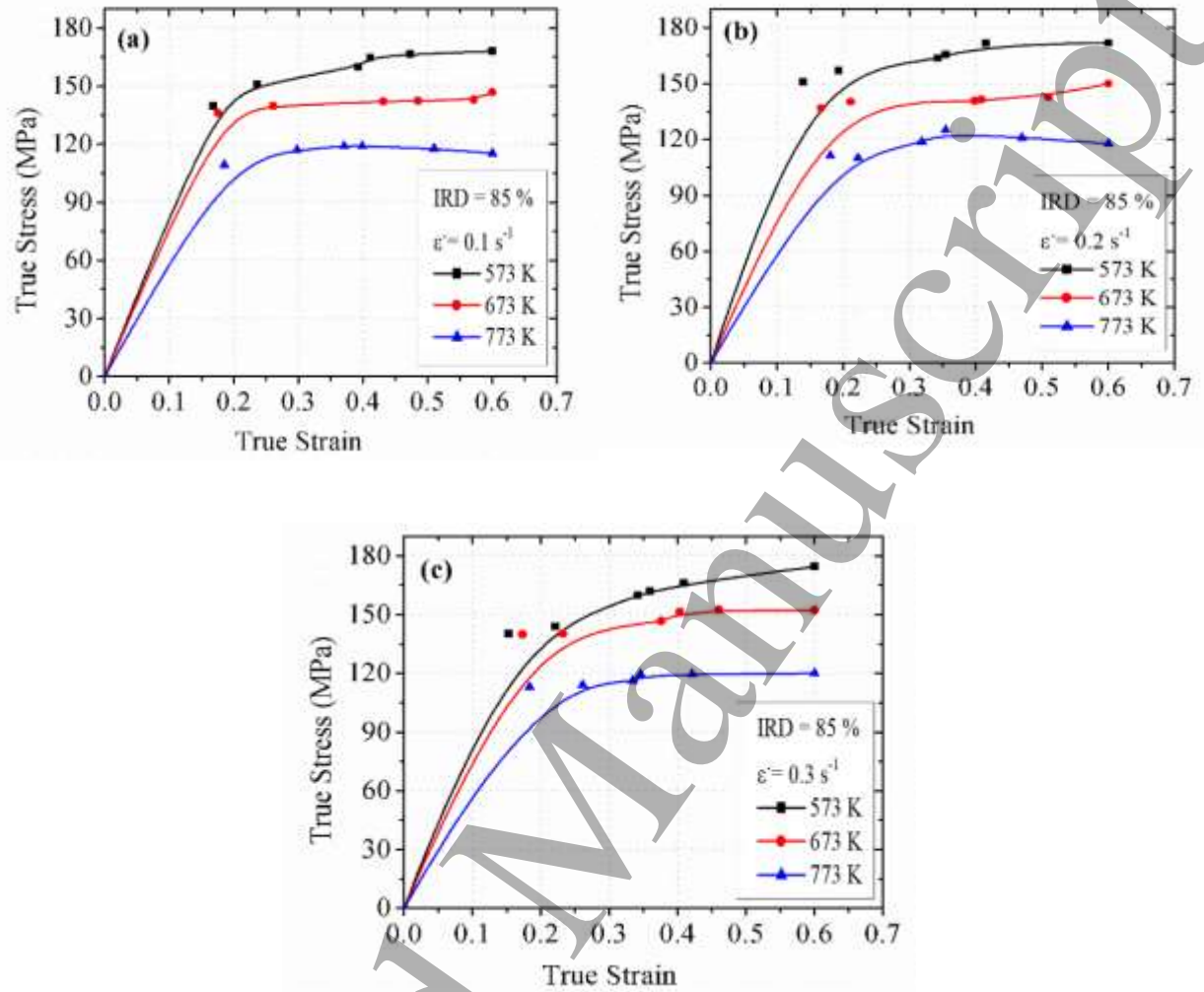


Figure. 3 True stress–true strain curves at various strain rate of Al-4%B<sub>4</sub>C composite with of 85%.

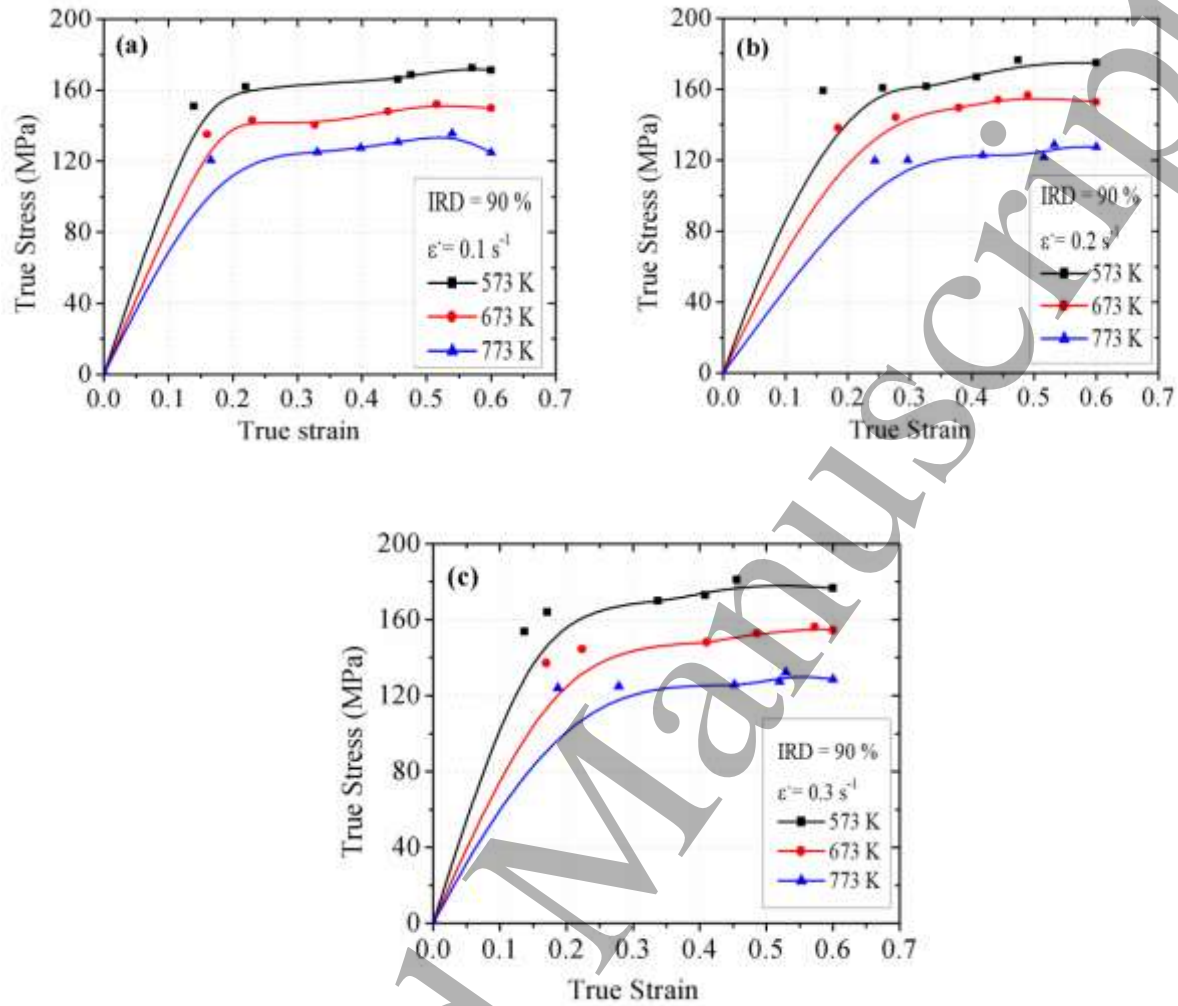


Figure. 4 True stress–true strain curves at various strain rate of Al–4%B<sub>4</sub>C composite with of 90%.

### 3.2. Development of constitutive model of Al–4%B<sub>4</sub>C composite

Generally, the Arrhenius equation is commonly adapted to describe the relationship between the flow stress and deformation condition [23, 24]. This equation could be expressed as follows:

$$\dot{\epsilon} = A [\sinh(\alpha\sigma)]^n \exp\left(-Q/RT\right) \quad (1)$$

Where  $\dot{\epsilon}$  = strain rate ( $s^{-1}$ );  $\sigma$  = flow stress (MPa);  $n$  = material constant;  $Q$  = activation energy of hot deformation ( $KJ\ mol^{-1}$ );  $R$  = universal gas constant ( $8.314\ J\ mol^{-1}\ K^{-1}$ );  $T$  = absolute temperature in Kelvin (K);  $A$  and  $\alpha$  are material constants.

For low stress levels ( $\alpha\sigma < 0.8$ ),  $\sinh(\alpha\sigma)^n \cong \alpha\sigma$ , for high stress levels ( $\alpha\sigma > 1.2$ ),  $\sinh(\alpha\sigma) \cong 0.5 \exp(\alpha\sigma)$  and hyperbolic sine law stress function can be used for any ( $\alpha\sigma$ ) values. Therefore, the Arrhenius equation can be rewritten as:

$$\dot{\epsilon} = A_1 \sigma^n \exp\left(-Q/RT\right) \quad [\alpha\sigma < 0.8] \quad (2)$$

$$\dot{\epsilon} = A_2 \exp(\beta\sigma) \exp\left(-Q/RT\right) \quad [\alpha\sigma > 1.2] \quad (3)$$

$$\dot{\epsilon} = A [\sinh(\alpha\sigma)]^n \exp\left(-Q/RT\right) \quad [\alpha\sigma \text{ taking any values}] \quad (4)$$

Where,  $A_1 = A\alpha^n$ ,  $A_2 = A/2^n$ , and  $\alpha = \beta/n$  are constants in which the  $\beta$  and  $n$  values are calculated from the experimental results.

Also, Zener and Hollomon [24] explained the effect of temperature and strain rate on hot deformation behavior can be evaluated through a single parameter  $Z$ , Zener–Holloman parameters ( $Z$ ):

$$Z = \dot{\epsilon} \exp\left(Q/RT\right) \quad (5)$$

By substituting equation (4) into the equation (5), it gives:

$$Z = A [\sinh(\alpha\sigma)]^n \quad (6)$$

Furthermore, the  $\sigma$  can also be written in terms of  $Z$  and material constants by solving equation (6), as per the hyperbolic sine function.

$$\sigma = \frac{1}{\alpha} \ln \left\{ \left( \frac{Z}{A} \right)^{\frac{1}{n}} + \left[ \left( \frac{Z}{A} \right)^{\frac{2}{n}} + 1 \right]^{\frac{1}{2}} \right\} \quad (7)$$

### 3.2.1. Calculation of material constants

As reported by Wolla et al. [10] that at higher temperatures, there is no effect of strain values on flow stress curves and it is remaining unchanged at higher values. As a result, the effect of strain on the development of above-mentioned equation (7) is not considered. Therefore, the material constants are determined at a strain value of 0.6 for sintered Al-4%B<sub>4</sub>C composite during the hot upsetting.

The equation. (8) and (9) are obtained from the equations. (2) and (3) by applying natural logarithm, respectively.

$$\ln \dot{\epsilon} = \ln A_1 + n \ln \sigma - \frac{Q}{RT} \quad (8)$$

$$\ln \dot{\epsilon} = \ln A_2 + \beta \sigma - \frac{Q}{RT} \quad (9)$$

At constant temperature, the hot upsetting process was carried hence the partial differentiation of equations (8) and (9) can be simplified as:

$$n = \left[ \frac{\partial \ln \dot{\epsilon}}{\partial \ln \sigma} \right]_{T=const} \quad (10)$$

$$\beta = \left[ \frac{\partial \ln \dot{\epsilon}}{\partial \sigma} \right]_{T=const} \quad (11)$$

The plots of  $\ln \dot{\epsilon} - \ln \sigma$  and  $\ln \dot{\epsilon} - \sigma$  are obtained by inserting the values of flow stress and corresponding strain rate for various temperatures and IRDes into equations (10) and (11) as shown in Figure. 5 and 6, respectively. From the average slope of the lines  $\ln \dot{\epsilon} - \ln \sigma$  and  $\ln \dot{\epsilon} - \sigma$  plots n and

$\beta$  values can be obtained for various temperatures, respectively. Therefore,  $\alpha = \beta/n$  value is calculated. The  $n$ ,  $\beta$  and  $\alpha$  values are tabulated in Table 1 for sintered Al-4%B<sub>4</sub>C composite during hot upsetting with different IRDes.

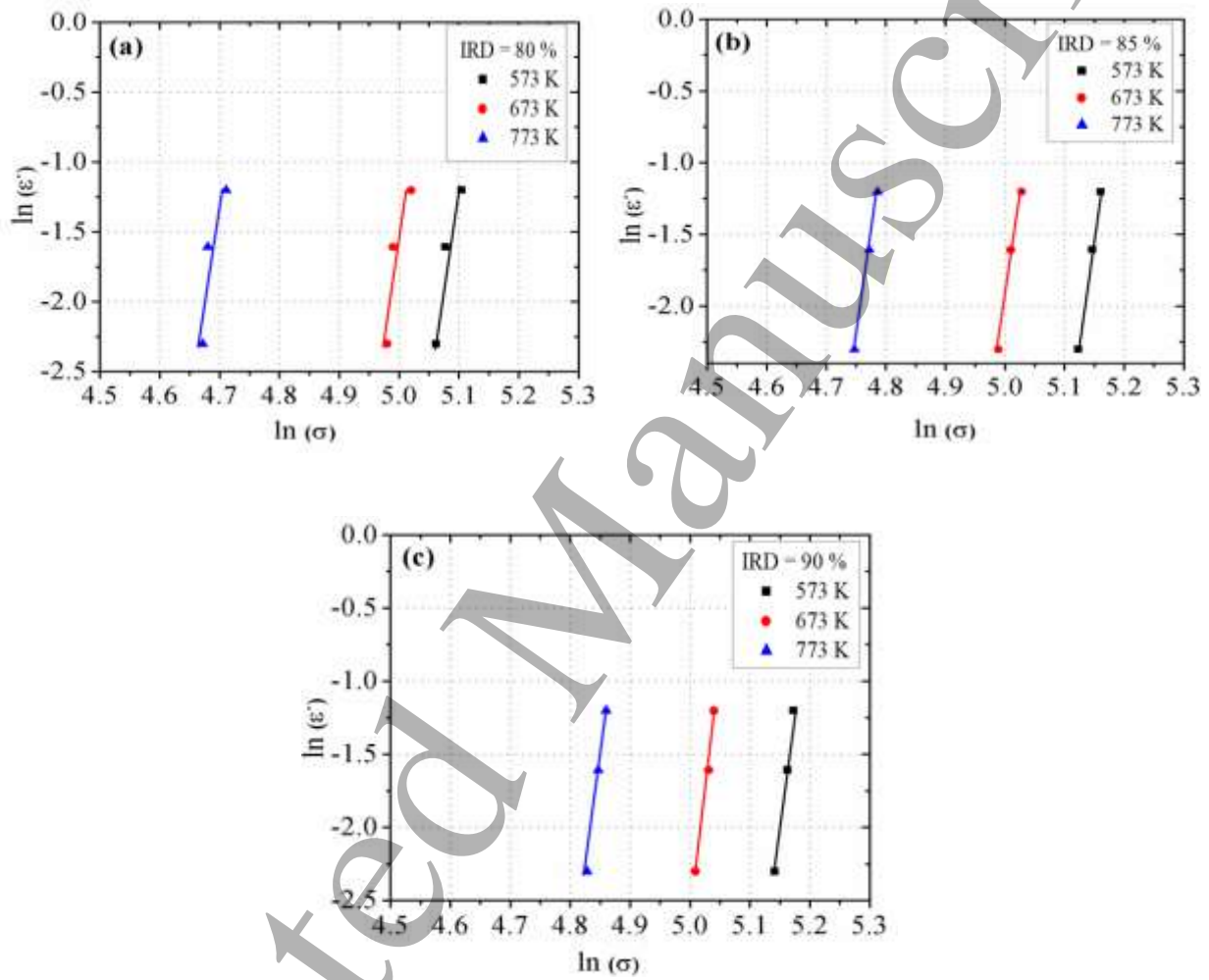


Figure. 5 Relationship between  $\ln \epsilon$ –  $\ln \sigma$  of Al-4%B<sub>4</sub>C composite

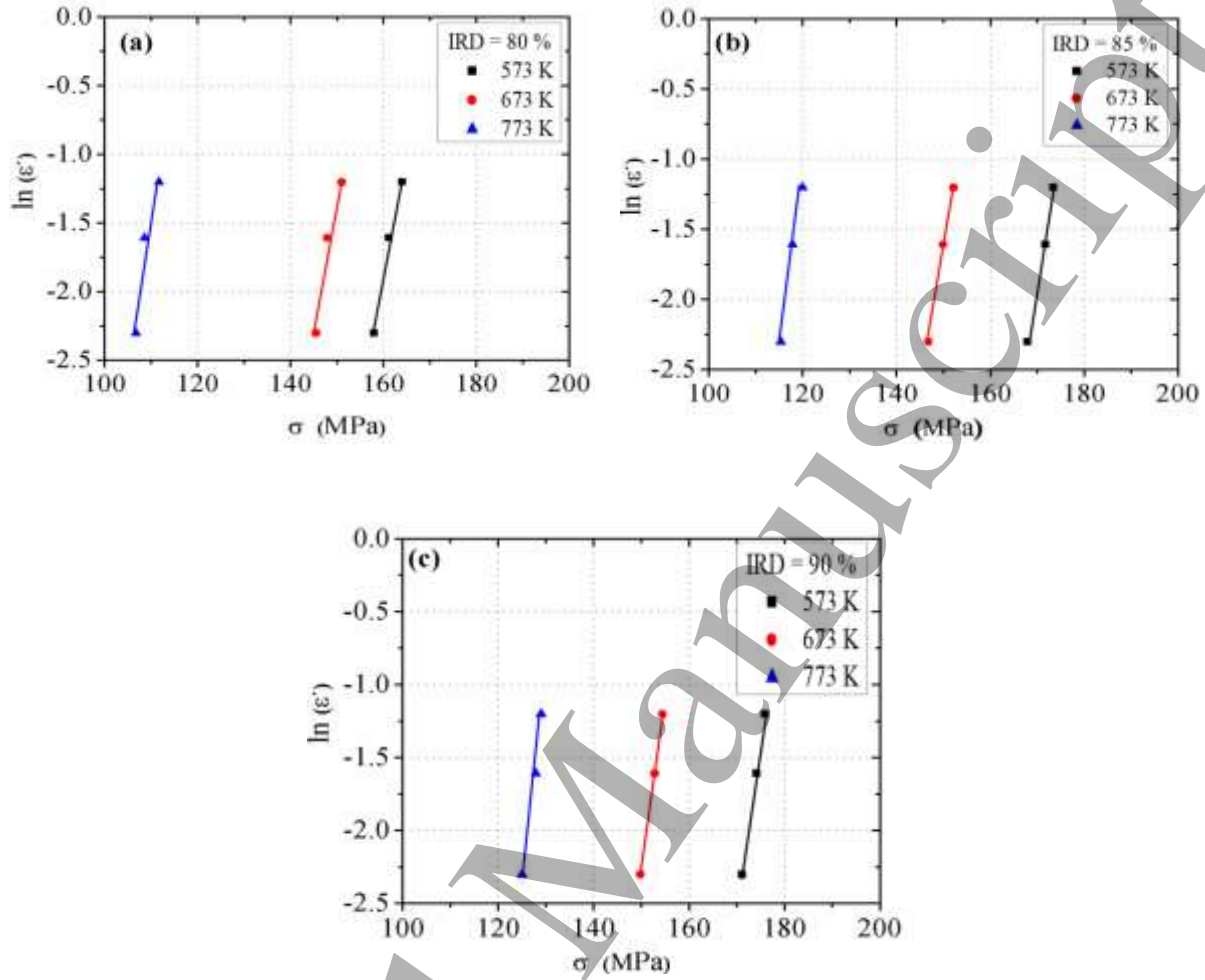


Figure. 6 Relationship between  $\ln\dot{\epsilon}$ - $\sigma$  of Al-4%B<sub>4</sub>C composite

Likewise, the activation energy ( $Q$ ) of sintered Al-4%B<sub>4</sub>C composite during hot upsetting with different IRDes can be obtained by applying the natural logarithm on both sides of equation

(4):

$$\ln \dot{\epsilon} = \ln A + n \ln[\sinh(\alpha\sigma)] - \frac{Q}{RT} \quad (12)$$

For the given constant strain rate condition, partial differentiation of equation (12) gives that:

$$Q = R \left\{ \frac{\partial \ln \dot{\epsilon}}{\partial \ln[\sinh(\alpha\sigma)]} \right\}_{T=const} \left\{ \frac{\partial \ln[\sinh(\alpha\sigma)]}{\partial \left(\frac{1}{T}\right)} \right\}_{\dot{\epsilon}=const} \quad (13)$$

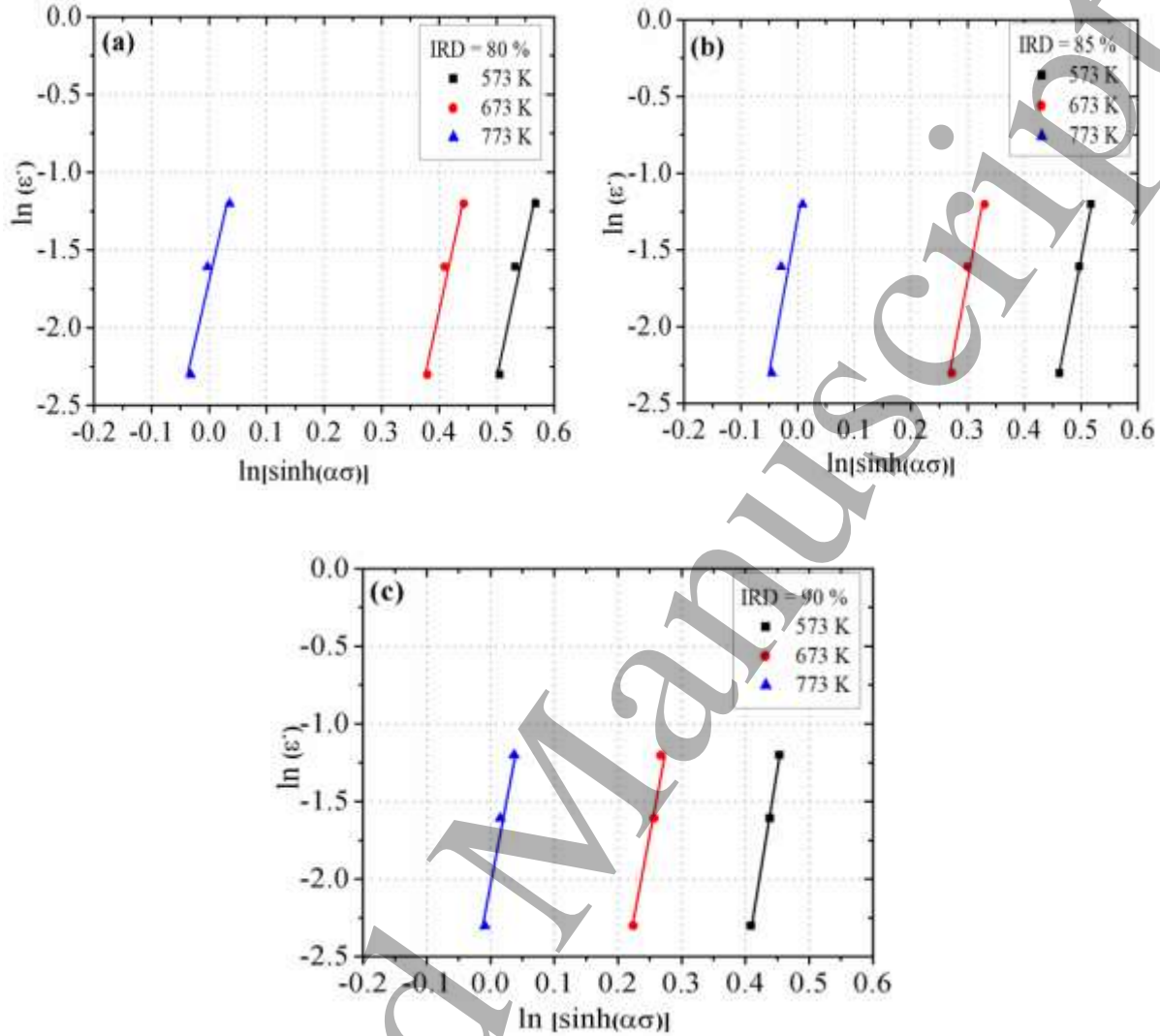


Figure. 7 Relationship between  $\ln\dot{\epsilon}$ – $\ln[\sinh(\alpha\sigma)]$  of Al–4%B<sub>4</sub>C composite

The relationship of  $\ln\dot{\epsilon}$ – $\ln[\sinh(\alpha\sigma)]$  and  $\ln[\sinh(\alpha\sigma)]$ – $1/T$  were obtained by inserting the values of  $\sigma$ ,  $\alpha$  and temperature and corresponding strain rate for different IRDes into equation (13), respectively. The  $Q$  values mentioned in Table 1 for different IRDes is obtained from the relation of  $\ln\dot{\epsilon}$ – $\ln[\sinh(\alpha\sigma)]$  and  $\ln[\sinh(\alpha\sigma)]$ – $1/T$  plots and are demonstrated in Figures. 7 and 8, respectively. It is noticed that the value of  $n$ ,  $\beta$ , and  $Q$  are greatly affected by the IRD. It is also noticed that the  $Q$  values for hot deformation decrease with decreasing IRD because of the presence of more pores in the preforms, which leads to a reduction in the resistance of the material



to deform. Also, the increase in IRD the Q values for hot deformation exhibited higher values. The activation energy is one of the key parameters which measures the degree of difficulty of the hot deformation of the materials. As a result, plastic deformations become more difficult with increasing IRD. The values of  $\alpha$  were decreased with an increase in the IRD.

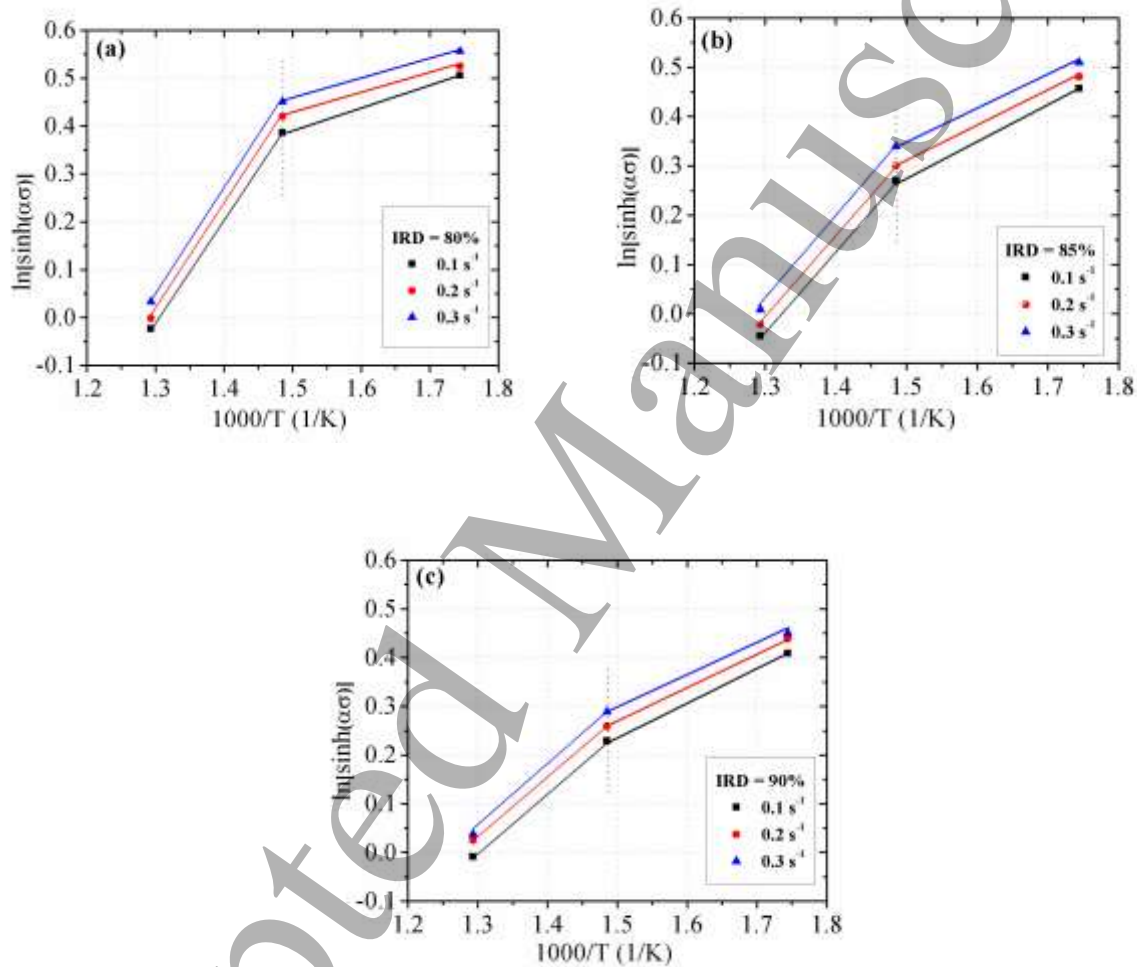


Figure. 8 Relationship between  $\ln [\sinh (\alpha \sigma)]-1 / T$  of Al-4%B<sub>4</sub>C composite

By applying the natural logarithm of equation (6), it gives:

$$\ln Z = \ln A + n \ln[\sinh(\alpha\sigma)] \quad (14)$$

By inserting the values of  $Q$  into equation (5),  $Z$  parameter can be evaluated. The values of  $\ln A$  determined from the intercept of lines  $\ln Z - \ln[\sinh(\alpha\sigma)]$  plots for different IRDes are demonstrated in Figure. 9. The values of  $\ln A$  for sintered Al-4%B<sub>4</sub>C composite with different IRDes of 80%, 85% and 90% can be found to be 21.27, 24.16 and 25.55, respectively.

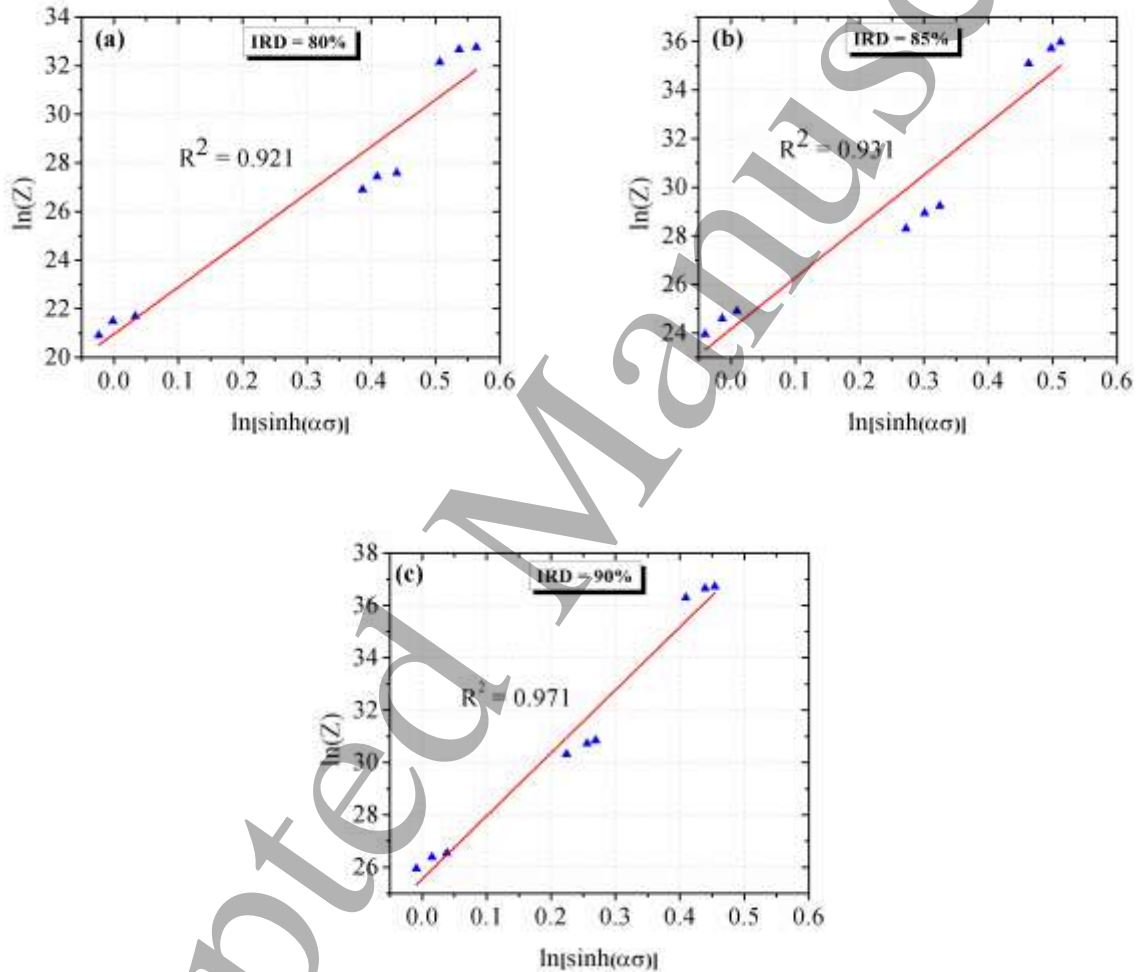


Figure. 9 Correlation between  $\ln Z - \ln[\sinh(\alpha\sigma)]$  of Al-4%B<sub>4</sub>C composite

Figure. 9 shows that the slope values of  $\ln Z - \ln[\sinh(\alpha\sigma)]$  plots are decreasing with a decrease in IRDes. When the slope of the plot  $\ln Z - \ln[\sinh(\alpha\sigma)]$  is low, the deformation conditions slightly affected PFS of the preforms, but it is significant for higher slope irrespective of the IRDes.

The relationship between  $n$ ,  $\alpha$ ,  $\ln A$  and  $Q$  and IRD of sintered Al-4%B<sub>4</sub>C composite were established by fitting data point into a polynomial function as shown in Figure. 10. Thus, the developed mathematical expression between IRD and flow stress, deformation temperature, strain rate of sintered Al-4%B<sub>4</sub>C composite during hot upsetting tests can be expressed as follows ( $R^2 =$  correlation coefficient):

$$n = 0.0422 \text{ IRD}^2 - 6.121 \text{ IRD} + 243.8 \quad (15)$$

$$\alpha = 6E - 06 \text{ IRD}^2 - 0.00113 \text{ IRD} + 0.0601 \quad (16)$$

$$Q = -0.049 \text{ IRD}^2 + 10.329 \text{ IRD} - 351.66 \quad (17)$$

$$\ln A = -0.03 \text{ IRD}^2 + 5.528 \text{ IRD} - 228.97 \quad (18)$$

Table 1. Values of  $\beta$ ,  $n$ ,  $\alpha$  and  $Q$  with different IRDes of Al-4%B<sub>4</sub>C composite

IRD (%)	$\beta$	$n$	$\alpha$	$Q$ (KJ/mol)
80	0.197	24.23	0.0081	161.06
85	0.212	28.44	0.0074	172.28
90	0.243	34.76	0.007	181.05

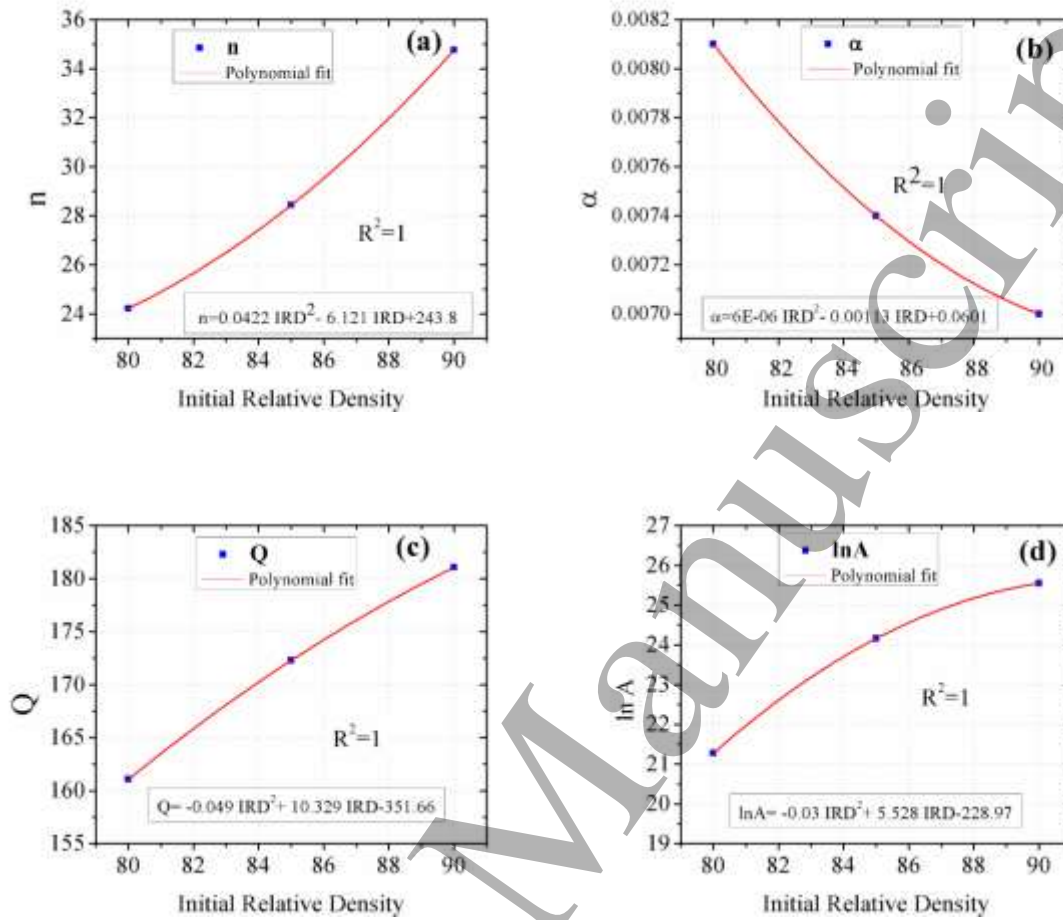


Figure. 10 Variations in (a)  $n$  (b)  $\alpha$  (c)  $Q$  (d)  $\ln A$  with initial relative density in sintered Al-4%B<sub>4</sub>C composite during hot upsetting test.

### 3.3. Validation of developed constitutive equations of Al-4%B<sub>4</sub>C composite

The predicted flow stress values determined according to equations. (7) and (15) – (18) is tabulated in Table 2. The values of predicted flow stress ( $\sigma_P$ ) are compared with experimental flow stress ( $\sigma_E$ ) values by plotting the graphs to assess the accuracy of the developed constitutive equation of sintered Al-4%B<sub>4</sub>C composite for different IRDes, and shown in Figure. 11. All the experimental and predicted data are close to the best fit line which indicates the accuracy of the

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3 constitutive equation. The  $R^2$  values are found to be 0.923, 0.977 and 0.994 for IRDes of 80%,  
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5 85%, and 90%, respectively.  
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9 Moreover, the established constitutive models for sintered Al-4%B<sub>4</sub>C composite accuracy  
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11 was confirmed by absolute error ( $\delta$ ) and mean absolute error ( $\delta_m$ ). The absolute error is calculated  
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13 from predicted and experimental values by using the equation (19).  
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$$\delta = \left| \frac{\sigma_P - \sigma_E}{\sigma_E} \right| \times 100 \% \quad (19)$$

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21 The detailed comparisons were made between the predicted and experimental results of sintered  
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23 Al-4%B<sub>4</sub>C composite for various temperatures and strain rates with different IRDes are shown in  
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25 Table 2. The absolute error does not exceed 10.6% and means absolute error does not exceed  
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27 9.95% for various IRDes and deformation conditions. The maximum mean absolute error is not  
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29 exceeding 9.95% and it is acceptable considering the complexity of the deformation behavior of  
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31 porous materials.  
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35 The established constitutive model has a good predictive capability for Al-4%B<sub>4</sub>C  
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37 composite during hot upsetting for all investigated temperatures and IRDes. Accordingly, the  
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39 predicted results are well satisfied with the experimental result, which verifies the accuracy of the  
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41 developed constitutive model for sintered Al-4%B<sub>4</sub>C composite during the hot upsetting test.  
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Table 2. Comparison between experimental and predicted peak flow stress of sintered Al-4%B<sub>4</sub>C composite

Def.	Tem. (K)	$\dot{\epsilon}$ (s <sup>-1</sup> )	IRD = 80%				IRD = 85%				IRD = 90%			
			$\sigma_E$ (MPa)	$\sigma_P$ (MPa)	$\delta$ (%)	$\delta_m$ (%)	$\sigma_E$ (MPa)	$\sigma_P$ (MPa)	$\delta$ (%)	$\delta_m$ (%)	$\sigma_E$ (MPa)	$\sigma_P$ (MPa)	$\delta$ (%)	$\delta_m$ (%)
	573	0.1	158.02	169.41	7.21		167.97	172.26	2.55		171.13	174.00	1.68	
	573	0.2	160.90	171.64	6.71	6.4	171.98	174.89	1.69	1.67	173.16	175.28	1.22	1.02
	573	0.3	164.32	173.11	5.35		174.68	176.02	0.77		175.24	175.22	0.16	
	673	0.1	145.54	134.26	7.75		146.81	136.49	7.03		150.26	144.37	3.92	
	673	0.2	147.67	136.42	7.67	8.1	149.93	138.86	7.39	7.54	151.61	145.68	3.91	4.27
	673	0.3	151.15	137.68	8.91		152.68	139.95	8.22		153.76	146.00	5.01	
	773	0.1	106.78	98.38	7.87		115.28	104.37	9.46		124.87	115.48	7.52	
	773	0.2	108.65	100.19	7.78	8.31	117.21	106.31	9.30	9.95	127.10	116.68	8.20	8.02
	773	0.3	111.71	101.34	9.28		119.97	107.24	10.6		127.81	117.11	8.37	

Further, the ability of the developed constitutive equation for predicting the peak flow stress of sintered Al-4%B<sub>4</sub>C composite was evaluated by calculating the peak flow stress with IRD of 88%. The predicted flow stress of sintered Al-4%B<sub>4</sub>C composite of 88% initial relative density for various temperatures and strain rates is compared with experimental peak flow stress of the same condition and as shown in Table 3. The experimental peak flow stress values of the sintered Al-4%B<sub>4</sub>C composite of 88% IRD were not used to develop the constitutive equation. It is noticed from Table 3 that the average mean absolute error is 5.97, which indicates the developed constitutive model was capable to predict accurately the peak flow stress of the performs.

Table 3. Comparison between experimental and predicted peak flow stress of sintered Al-4%B<sub>4</sub>C composite of initial relative density 88%

Def.	Tem. (K)	$\dot{\epsilon}$ (s <sup>-1</sup> )	IRD = 88%			$\delta_m$ (%)
			$\sigma_E$ MPa	$\sigma_P$ MPa	$\delta$ (%)	
	573	0.1	169.25	156.61	7.46	7.97
	573	0.2	173.17	159.07	8.13	
	573	0.3	175.15	160.52	8.34	
	673	0.1	148.41	137.59	7.28	7.49
	673	0.2	151.17	139.90	7.45	
	673	0.3	153.12	141.25	7.74	
	773	0.1	122.08	124.37	1.88	2.47
	773	0.2	123.26	126.55	2.67	
	773	0.3	124.25	127.83	2.88	
Average						5.97

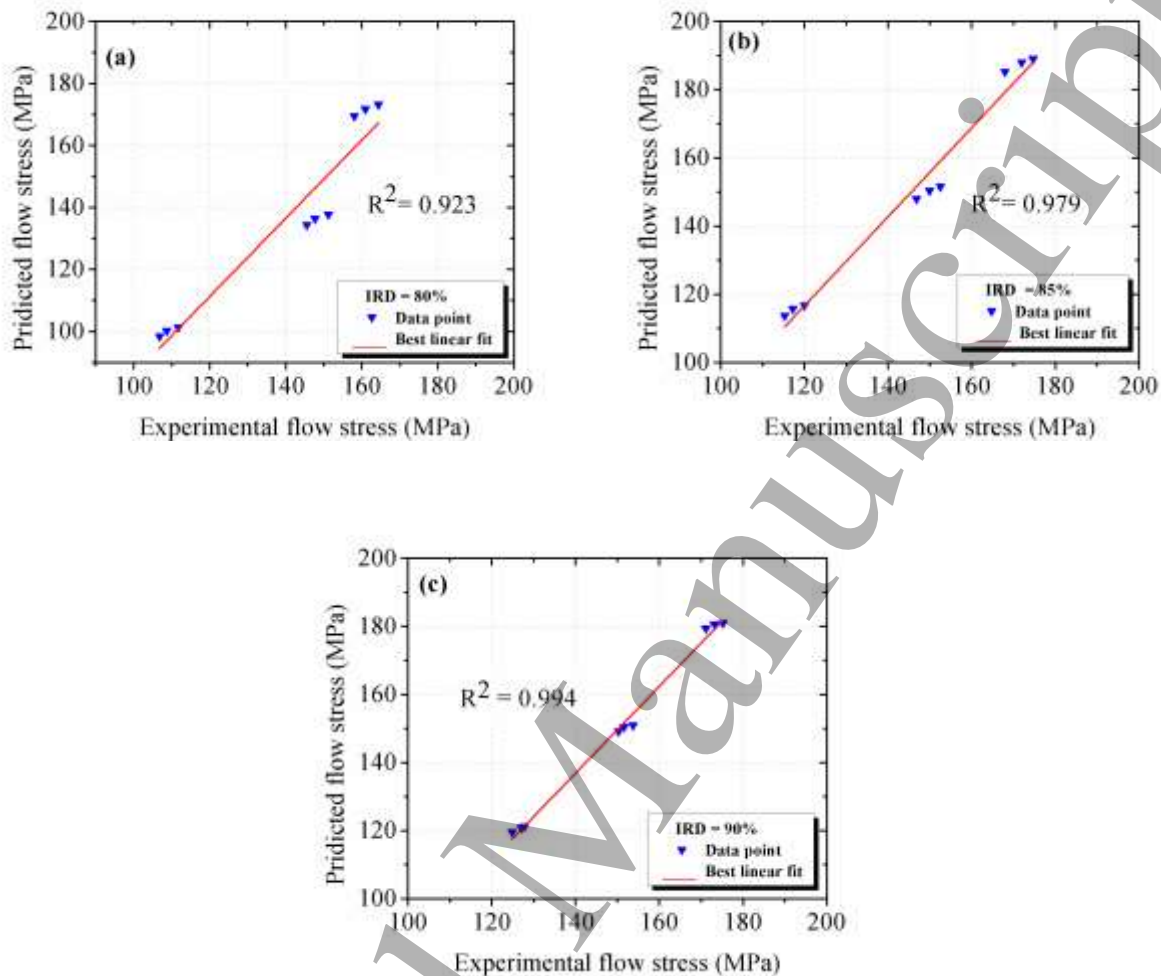


Figure. 11 Correlation between experimental and predicted results of sintered Al-4%B<sub>4</sub>C composite

#### 4. Activation energy of sintered Al-4%B<sub>4</sub>C composite

The average activation energy ( $Q$ ) of sintered Al-4%B<sub>4</sub>C composite was calculated for various IRDes during the hot upsetting test, which is higher than the value of pure aluminum as shown in Table 4. It was reported [25, 26] that the activation energy of aluminum metal matrix composite for hot deformation was higher than that of aluminum. The dislocation motion is impeded by the existing B<sub>4</sub>C particles in the composite. It was concluded that the obtained activation energy of



sintered Al-4%B<sub>4</sub>C preforms for different IRDes is acceptable. The occurrence of higher activation energy during the upsetting tests of composite materials is due to the transformation of the deformation load to reinforcement by the matrix [25, 26], whereby an interfacial diffusion is considerably slower, which increases the activation energy of composite materials.

Table 4. Activation energies (Q) (KJ/mol) for different compositions

Composition	Fabrication Route	Activation energy (Q)			Reference
		(KJ/mol)			
Al-4%B <sub>4</sub> C	Powder metallurgy	IRD			Present investigation
		80%	85%	90%	
		161.08	172.28	181.05	
Pure aluminum	Casting	144.3			[27]

## 5. Conclusions

The hot deformation behavior of sintered Al-4%B<sub>4</sub>C composite with various IRDes of 80%, 85%, and 90% was studied by performing the hot upsetting test for various temperatures of 573 K, 673 K and 773 K and strain rates of 0.1 s<sup>-1</sup>, 0.2 s<sup>-1</sup> and 0.3 s<sup>-1</sup>. The following conclusion can be drawn:

1. The influences of the IRD and deformation conditions on the  $\sigma$ - $\epsilon$  curves are significant for all tested conditions. The flow stress curves increase with increasing IRD and strain rate, whereas decreases with deformation temperature.

2. The IRD has a great influence on the hot deformation behavior of sintered Al-4%B<sub>4</sub>C composite. The activation energy of hot deformation was exhibited at higher values due to an increase in IRD.
3. The constitutive equations were developed between material constants and IRD for predicting the flow stress of sintered Al-4%B<sub>4</sub>C composite precisely.
4. The comparison was made between the predicted and experimental values and it shows good agreement. The absolute errors were not exceeding 10.6% and mean absolute error does not exceed 9.95% for various IRDes and deformation conditions.
5. The activation energy (Q) calculated for sintered Al-4%B<sub>4</sub>C composite with IRDes of 80%, 85%, and 90% was 161.06, 172.28 and 181.05 KJ/mol, respectively. This range of values is higher than the value of pure aluminum (144.3 KJ/mol).

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